

Surds 1

To be able to simplify surds

No Calculator

Mini WB

(Q1) Write below as index form

$$\frac{1}{y^n}$$

Connect

(Q2) Write below as a fraction

$$2x^{-2}$$

(Q3) Express as a power of 2:

$$16$$

(Q4)

$$\left(\frac{81}{16}\right)^{-\frac{3}{4}}$$

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(Q1) Write below as index form

$$\frac{1}{y^n}$$

$$y^{-n}$$

Connect

(Q2) Write below as a fraction

$$2x^{-2} \quad \frac{2}{x^2}$$

(Q3) Express as a power of 2:

$$16$$

$$2^4$$

(Q4)

$$\left(\frac{81}{16}\right)^{-\frac{3}{4}}$$

$$\frac{8}{27}$$

Activate

Real Numbers

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graph TD; A[Real Numbers] --> B[Rational Numbers]; A --> C[Irrational Numbers]
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Real numbers are any possible decimal or whole number.

Rational Numbers

are all numbers which can be expressed as some fraction involving integers (whole numbers), e.g. $\frac{1}{4}$, $3\frac{1}{2}$, -7 .

Irrational Numbers

are real numbers which are not rational.

What is a surd?

A surd is a root of a number that cannot be simplified to a rational number.

$$\sqrt{2}$$

Not a surd

Surd

$$\sqrt{9}$$

Not a surd

Surd

$$\sqrt{5}$$

Not a surd

Surd

$$\sqrt{\frac{1}{4}}$$

Not a surd

Surd

$$\sqrt[3]{7}$$

Not a surd

Surd

What is a surd?

A surd is a root of a number that cannot be simplified to a rational number.

ANSWER

	Not a surd	Surd
$\sqrt{2}$	<input checked="" type="checkbox"/>	<input checked="" type="checkbox"/>
$\sqrt{9}$	<input checked="" type="checkbox"/>	<input checked="" type="checkbox"/>
$\sqrt{5}$	<input checked="" type="checkbox"/>	<input checked="" type="checkbox"/>
$\sqrt{\frac{1}{4}}$	<input checked="" type="checkbox"/>	<input checked="" type="checkbox"/>
$\sqrt[3]{7}$	<input checked="" type="checkbox"/>	<input checked="" type="checkbox"/>

Laws of Surds

$$\sqrt{a} \times \sqrt{b} = \sqrt{ab}$$

Examples:

$$\begin{aligned} & \sqrt{3} \times \sqrt{2} \\ &= \sqrt{3 \times 2} \\ &= \sqrt{6} \end{aligned}$$

$$\sqrt{x^2} = x$$

Examples:

$$\begin{aligned} & \sqrt{4x^2} \\ &= \sqrt{4} \sqrt{x^2} \\ &= 2x \end{aligned}$$

Activate

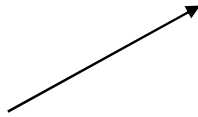
$$\frac{\sqrt{a}}{\sqrt{b}} = \sqrt{\frac{a}{b}}$$

Examples:

$$\begin{aligned} & \sqrt{\frac{1}{9}} \\ &= \frac{\sqrt{1}}{\sqrt{9}} \\ &= \frac{1}{3} \end{aligned}$$

Simplifying Surds

$$\sqrt{8} = \sqrt{4}\sqrt{2} = 2\sqrt{2}$$



Could we somehow use $\sqrt{ab} = \sqrt{a}\sqrt{b}$ to break the 8 up in a way that one of the surds will simplify?

Method 1: Find the largest square factor of the number, and put that first.

$$\sqrt{27} =$$

?

$$\sqrt{32} =$$

?

$$2\sqrt{50} =$$

?

$$4\sqrt{12} =$$

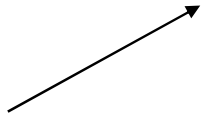
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Activate

Method 2: Write the number as a product of its prime.

Simplifying Surds

$$\sqrt{8} = \sqrt{4}\sqrt{2} = 2\sqrt{2}$$



Could we somehow use $\sqrt{ab} = \sqrt{a}\sqrt{b}$ to break the 8 up in a way that one of the surds will simplify?

Method 1: Find the largest square factor of the number, and put that first.

$$\sqrt{27} = \sqrt{9}\sqrt{3} = 3\sqrt{3}$$

$$\sqrt{32} = \sqrt{16}\sqrt{2} = 4\sqrt{2}$$

ANSWER

$$2\sqrt{50} = 2\sqrt{25}\sqrt{2} = 10\sqrt{2}$$

$$4\sqrt{12} = 4\sqrt{4}\sqrt{3} = 8\sqrt{3}$$

Activate

Method 2: Write the number as a product of its prime.

MINI WB

Demonstrate

(Q1) Simplify the following:

$$\sqrt{75} = \boxed{\quad ? \quad}$$

(Q2) Simplify the following:

$$\sqrt{20} = \boxed{\quad ? \quad}$$

(Q3) Simplify the following:

$$\sqrt{48} = \boxed{\quad ? \quad}$$

(Q4) Simplify the following:

$$3\sqrt{200} = \boxed{\quad ? \quad}$$

ANSWER

Demonstrate

(Q1) Simplify the following:

$$\sqrt{75} = \sqrt{25}\sqrt{3} = 5\sqrt{3}$$

(Q2) Simplify the following:

$$\sqrt{20} = \sqrt{4}\sqrt{5} = 2\sqrt{5}$$

(Q3) Simplify the following:

$$\sqrt{48} = \sqrt{16}\sqrt{3} = 4\sqrt{3}$$

(Q4) Simplify the following:

$$3\sqrt{200} = 3\sqrt{100}\sqrt{2} = 30\sqrt{2}$$

Do them in your book and show all the steps

Demonstrate

1 Simplify the following:

a $\sqrt{8} =$

b $\sqrt{18} =$

c $\sqrt{50} =$

d $\sqrt{80} =$

e $\sqrt{72} =$

2 Simplify the following:

a $5\sqrt{80} =$

b $2\sqrt{125} =$

c $8\sqrt{12} =$

d $3\sqrt{72} =$

e $2\sqrt{28} =$

ANSWER

Demonstrate

1 Simplify the following:

a $\sqrt{8} = 2\sqrt{2}$

b $\sqrt{18} = 3\sqrt{2}$

c $\sqrt{50} = 5\sqrt{2}$

d $\sqrt{80} = 4\sqrt{5}$

e $\sqrt{72} = 6\sqrt{2}$

2 Simplify the following:

a $5\sqrt{80} = 20\sqrt{5}$

b $2\sqrt{125} = 10\sqrt{5}$

c $8\sqrt{12} = 16\sqrt{3}$

d $3\sqrt{72} = 18\sqrt{2}$

e $2\sqrt{28} = 4\sqrt{7}$